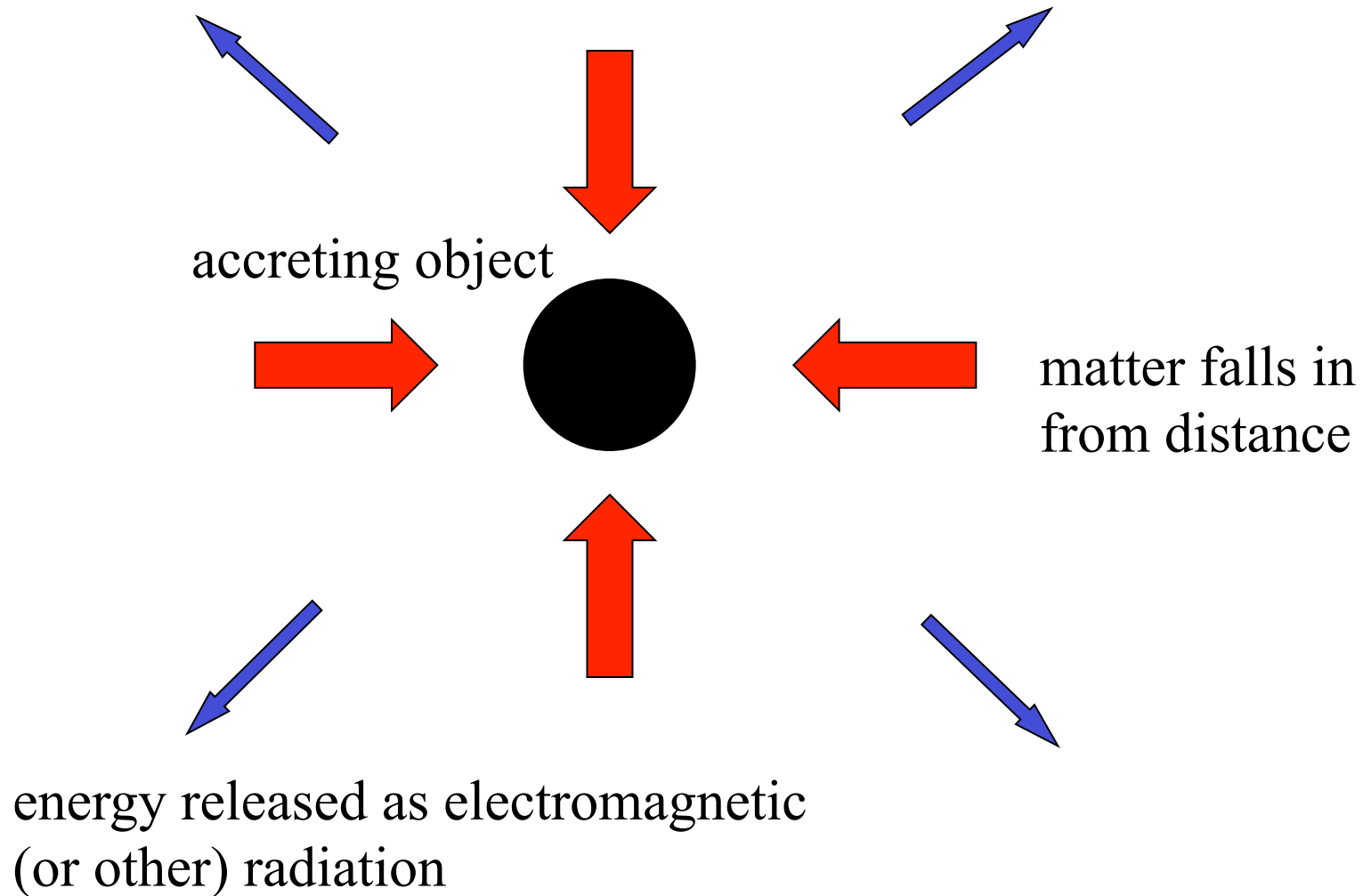


# Accretion

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accretion = release of gravitational energy from infalling matter



but **accreting matter always has (specific) angular momentum**

$$j \sim (GM R_0)^{1/2}$$

where  $M$  is gravitating mass at radius  $R_0$  from accretor

so even if destabilized it hangs up centrifugally at some radius

$$R_{\text{circ}} \sim \left( \frac{j^2}{GM_{\text{accretor}}} \right)^{1/2} \sim f R_0 \gg R_{\text{accretor}}$$

e.g in a close binary,  $R_{\text{circ}} \sim$  binary separation

feeding AGN: infalling matter has  $R_{\text{circ}} \gg R_s$  (SMBH)

*must lose angular momentum in order to accrete*

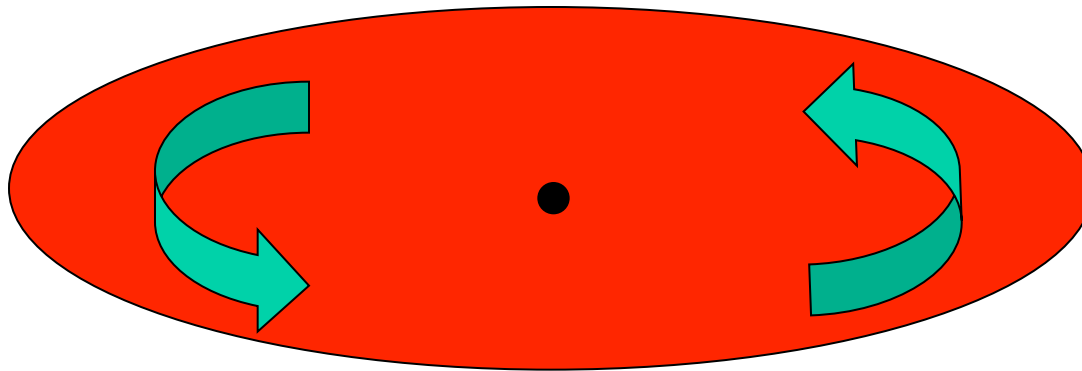
so

1. spherical (Bondi) accretion is never a good approximation
2. accretion is *always* from a disc:

energy losses via dissipation are always faster than a.m. losses,  
and orbit of lowest energy for fixed angular momentum is a  
circle

matter spirals in through a sequence of circular orbits.

this is an *accretion disc* – thickness  $H$  is smaller than radius  $R$



*accretion discs are universal*

*condition for a thin disc ( $H \ll R$ )*

disc is almost hydrostatic in z-direction, so



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$$\frac{1}{\rho} \frac{\partial P}{\partial z} = \frac{\partial}{\partial z} \left( \frac{GM}{(R^2 + z^2)^{1/2}} \right)$$

but if the disc is thin,  $z \ll R$ , so this is

$$\frac{1}{\rho} \frac{\partial P}{\partial z} = - \frac{GMz}{R^3}$$

with  $\partial P/\partial z \sim P/H$ ,  $z \sim H$  and  $P \sim \rho c_s^2$ , where  $c_s$  is sound speed, we find

$$H \sim c_s \left( \frac{R}{GM} \right)^{1/2} \sim \frac{c_s}{v_K} R$$

hence *thin disc requires Kepler velocity to be highly supersonic*

since  $c_s \propto T^{1/2}$ , *this requires that the disc can cool.*

if this holds we can also show that

*the azimuthal velocity is close to Kepler*

so for discs,

**thin**  $\longleftrightarrow$  **Keplerian**  $\longleftrightarrow$  **efficiently cooled**

*either all three of these properties hold, or none do!*



need some means of removing angular momentum: *viscosity*

early parametrization  $v \sim \lambda u$  with typical length and velocity scales  $\lambda, u$ . Now argue that

$$\lambda < H, u < c_s$$

first relation obvious, second because supersonic random motions would shock. Thus set

$$v = \alpha c_s H$$

and argue that  $\alpha < 1$ , *but* no reason to suppose  $\alpha = \text{const}$

'alpha—prescription' useful because disc structure only depends on low powers of  $\alpha$  - but *no predictive power*

surface density of disc changes diffusively on **viscous timescale**

$$t_{\text{visc}} = \frac{R^2}{\nu} = \left( \frac{R}{H} \right)^2 \frac{1}{\alpha \Omega}$$

AGN disc:  $H/R \sim 10^{-3}$ ,  $\Omega(R) = (GM/R^3)^{1/2}$ , so

$$t_{\text{visc}} \sim 5 \times 10^{10} R_{\text{pc}}^{3/2} M_8^{-1/2} \text{ yr!}$$

$$(R_{\text{pc}} = R/(\text{pc}), M_8 = M/10^8 M_{\odot})$$

-- gas feeding AGN must have tiny a.m. *before* forming a disc

*physical* angular momentum transport

a disc has

$$\frac{\partial}{\partial R} (R^2 \Omega) > 0, \quad \text{but} \quad \frac{\partial \Omega}{\partial R} < 0$$

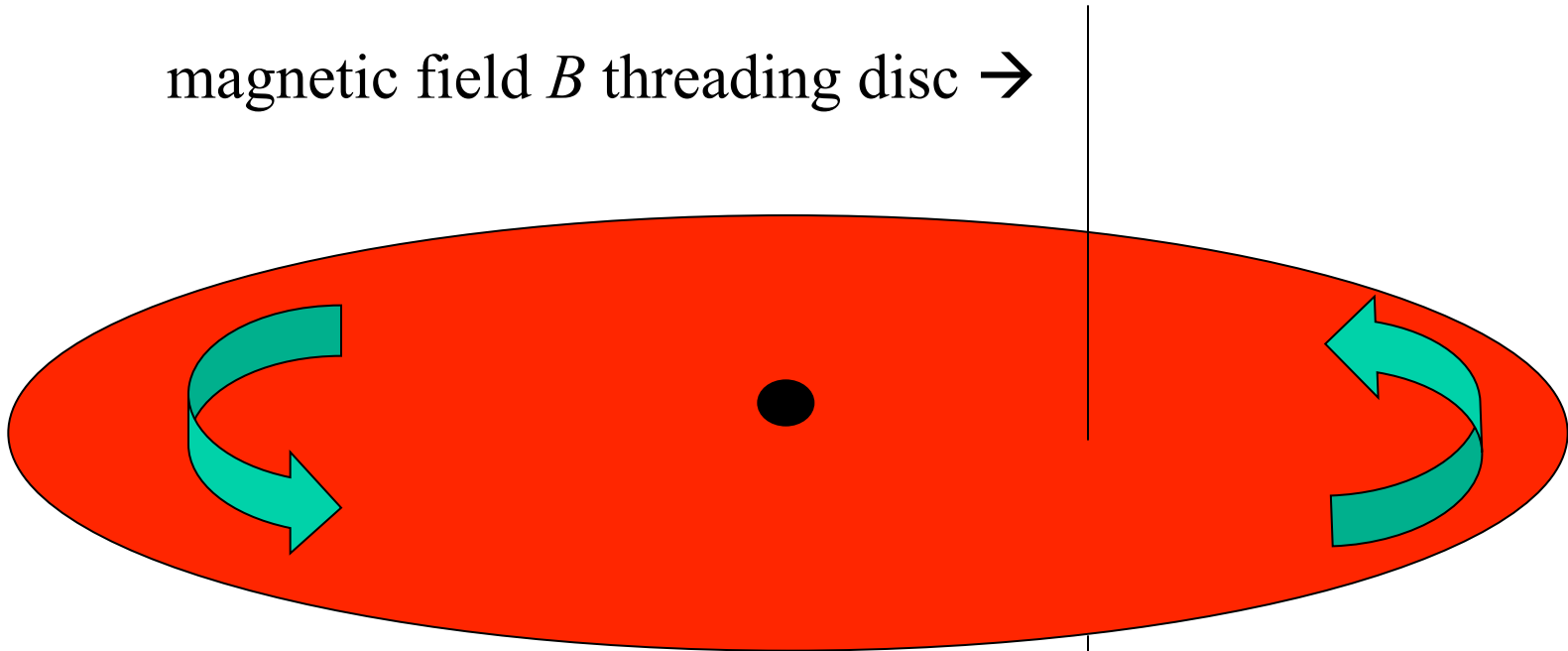
accretion requires a mechanism to transport a.m. outwards, but first relation  $\rightarrow$  *stability* against axisymmetric perturbations (Rayleigh criterion).

most potential mechanisms sensitive to a.m. gradient, so transport a.m. *inwards*!

need a mechanism sensitive to  $\Omega$  or  $v_K$

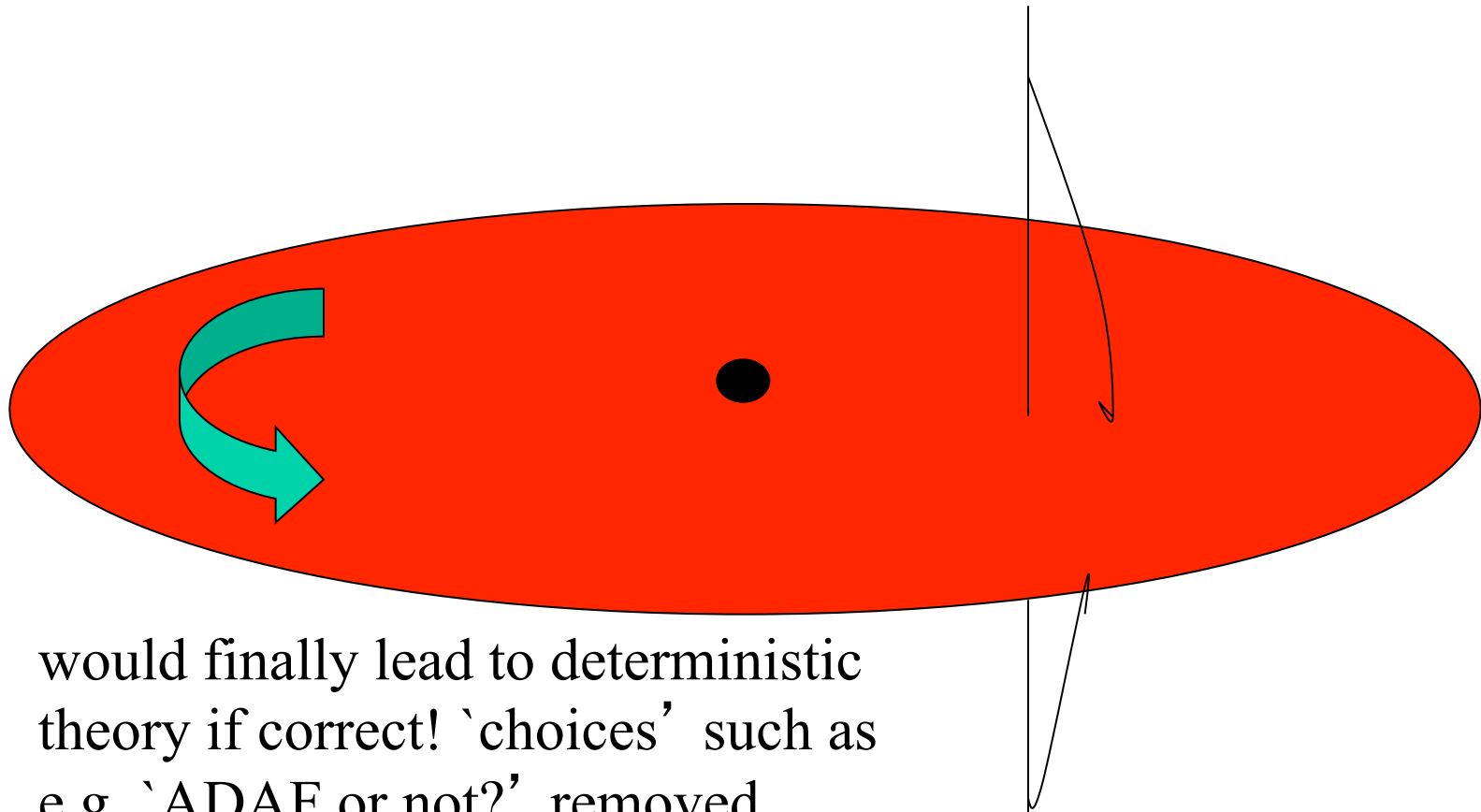
*Balbus—Hawley (magnetorotational, MRI) instability*

magnetic field  $B$  threading disc  $\rightarrow$



magnetic tension tries to *straighten* line  
imbalance between gravity and rotation *bends* line

vertical fieldline perturbed outwards, rotates faster than surroundings, so centrifugal force  $>$  gravity  $\rightarrow$  *kink increases*.  
line connects fast-moving (inner) matter with slower (outer) matter, and speeds latter up: *outward a.m. transport*

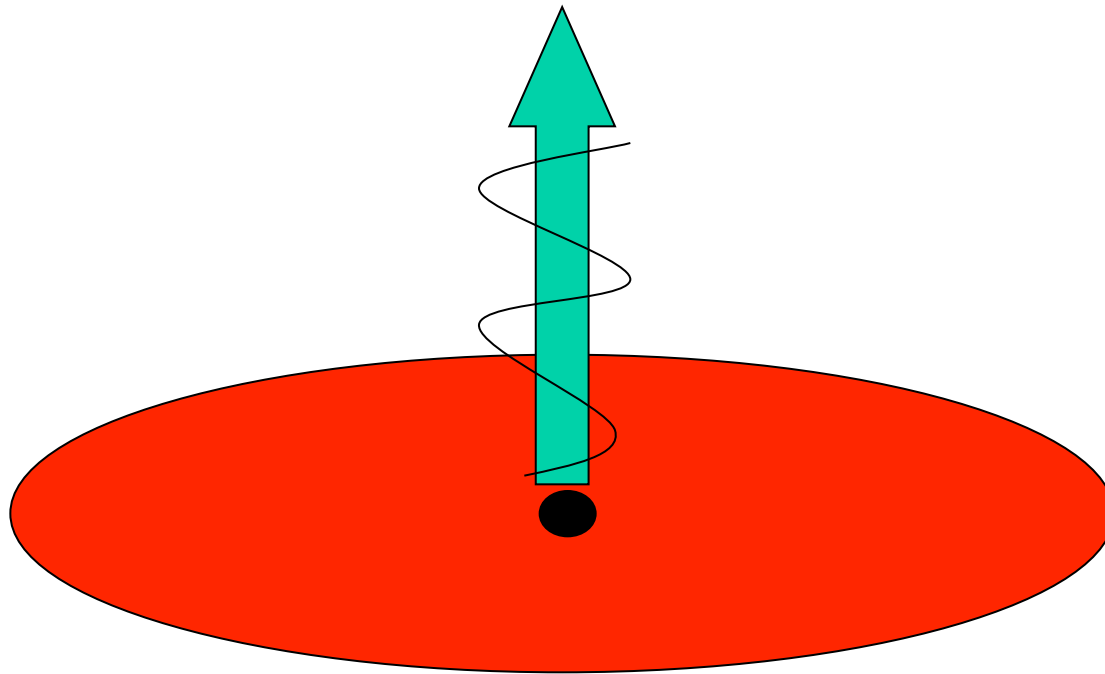


would finally lead to deterministic theory if correct! 'choices' such as e.g. 'ADAF or not?' removed

## *Jets*

one observed form of outflow: jets with  $\sim$  escape velocity from point of ejection,  $\sim c$  for black holes

launching and collimation not understood – but Lorentz factors  $\gamma \gg 1$  probably require toroidal magnetic field, since

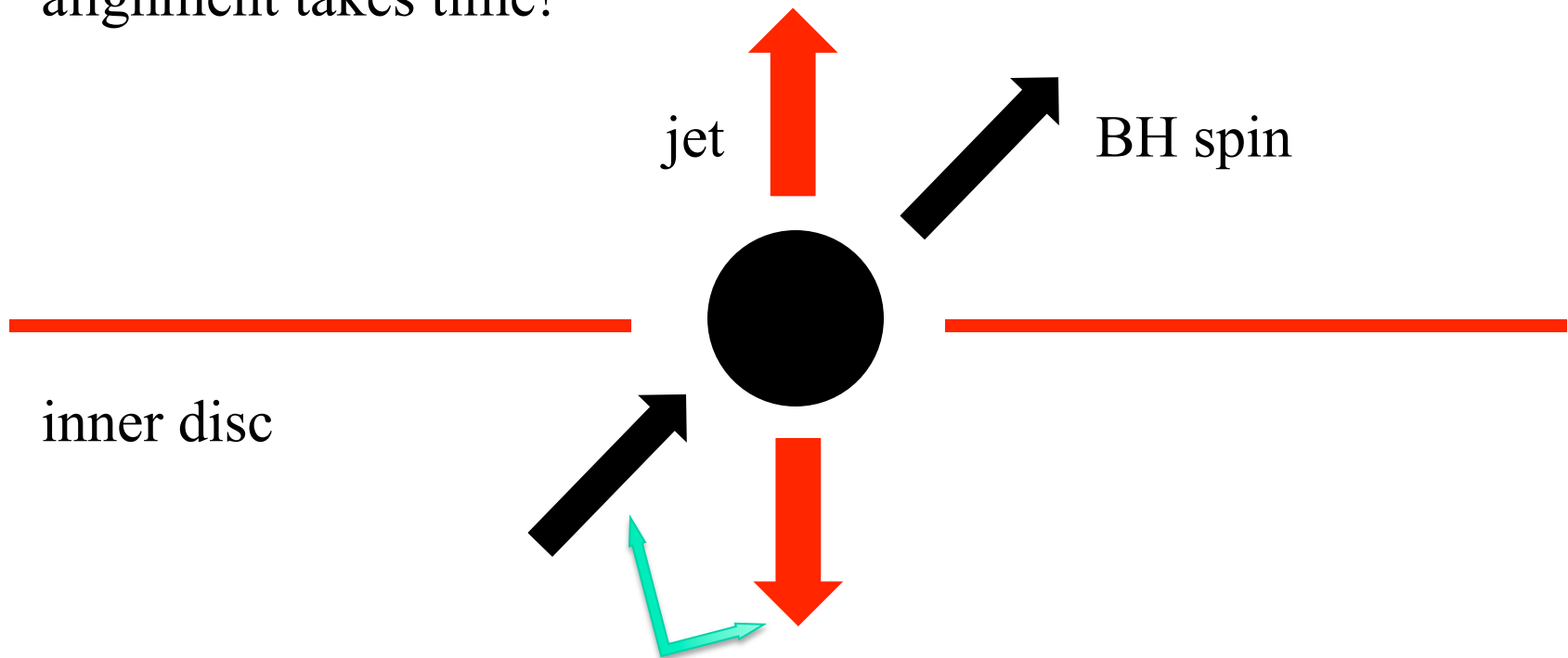


disc must choose to put a lot of energy into little matter

jets generally come from deepest part of potential – near accretor,

so **jet direction is orthogonal to plane of inner disc**

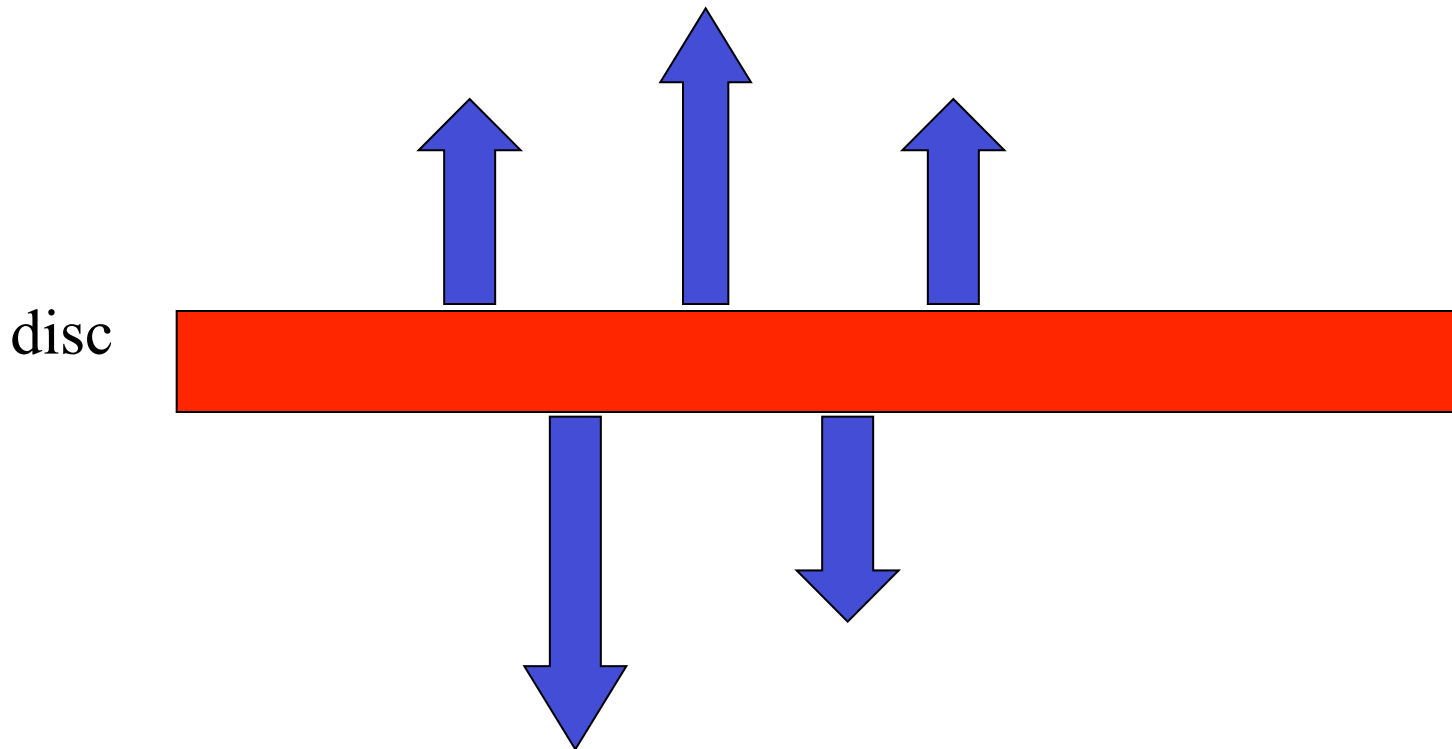
*this does **not** need to be the same as the BH spin direction:  
alignment takes time!*



disc – spin alignment via Lense–Thirring effect + dissipation

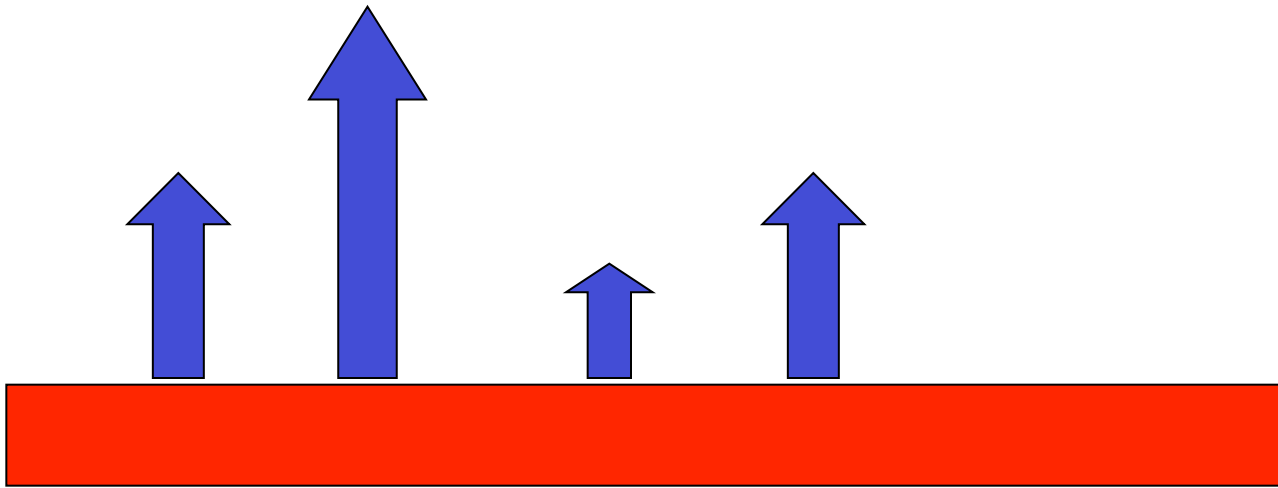
disc may have *two* states:

1. infall energy goes into radiation (standard)
2. infall energy goes into winding up internal disc field – thus



generally vertical field directions uncorrelated in neighboring disc annuli (dynamo random); BUT





occasionally all fields line up  $\rightarrow$  matter swept inwards, strengthens field  $\rightarrow$  energy all goes into field  $\rightarrow$  jet ???

(e.g. King, Pringle, West, Livio, 2004)

*jets seen (at times) in almost all accreting systems: AGN, LMXBs etc*

accretion produces radiation: radiation makes pressure – can this inhibit further accretion?

radiation pressure acts on electrons; but electrons and ions (protons) cannot separate because of Coulomb force: **radiation pressure force** on an electron is

$$F_{\text{rad}} = \frac{L\sigma_T}{4\pi cr^2}$$

(in spherical symmetry).

**gravitational force** on electron—proton pair is

$$F_{\text{grav}} = \frac{GMm_p}{r^2} \quad (m_e \ll m_p)$$

thus accretion is inhibited once  $F_{\text{rad}} > F_{\text{grav}}$ , i.e. once

$$L > L_{\text{Edd}} = \frac{4\pi GMc}{\kappa} = 1.3 \times 10^{38} \frac{M}{M_{\odot}} \text{ erg s}^{-1}$$

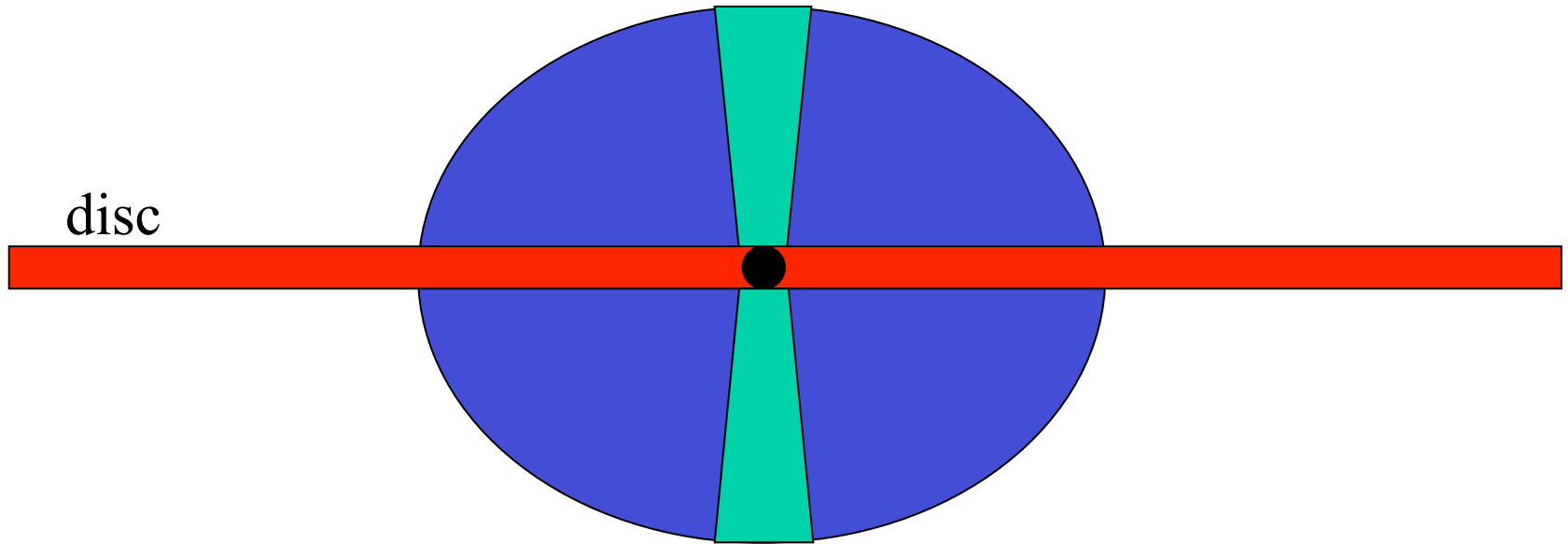
( $\kappa \simeq \sigma_T/m_p =$  opacity  $\gtrsim$  electron scattering)

so what happens if accretor is fed at rates

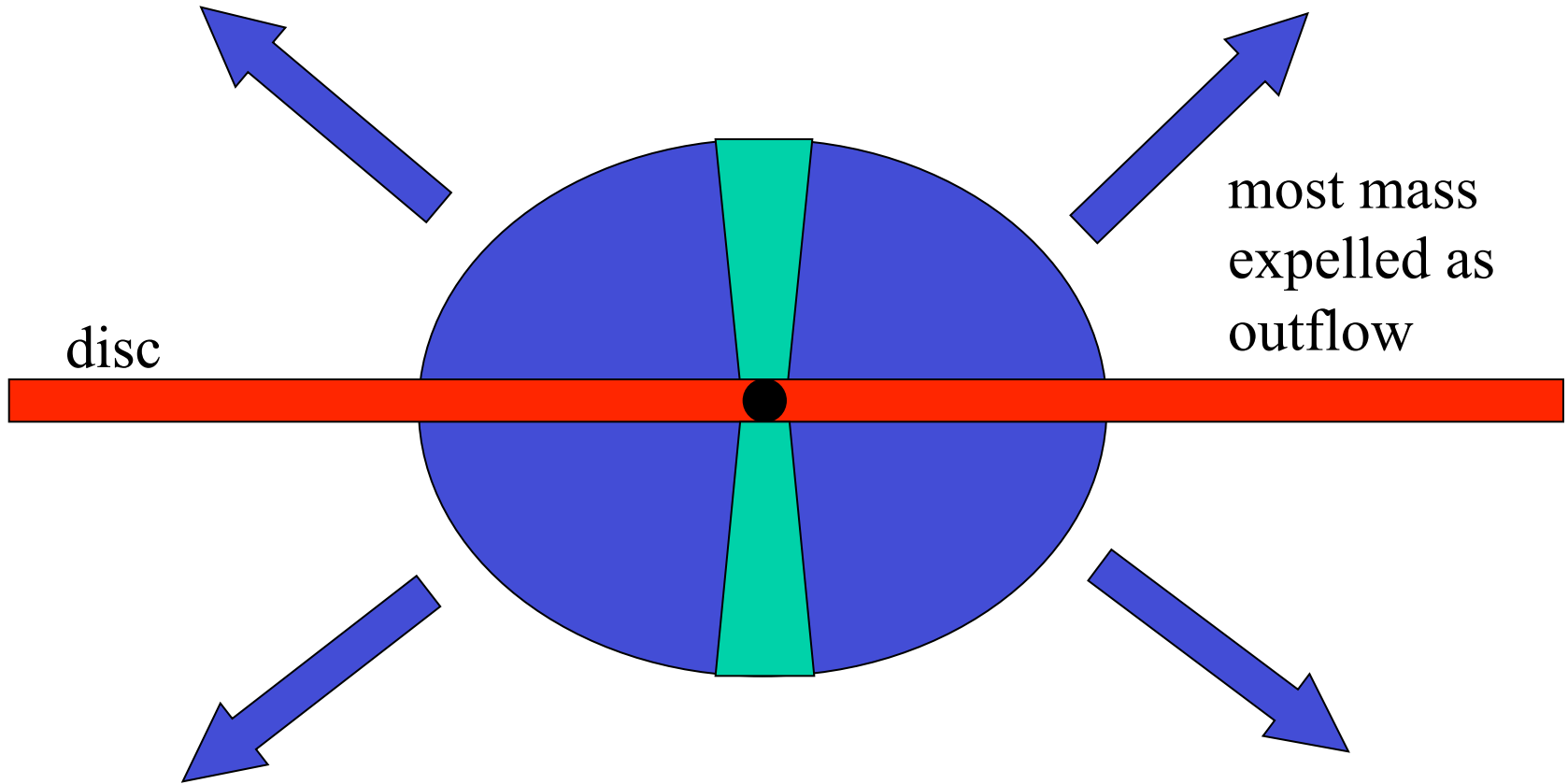
$$\dot{M} > \dot{M}_{\text{Edd}} = L_{\text{Edd}}/\eta c^2 ?$$

# Super-Eddington Accretion

(Shakura & Sunyaev, 1973)

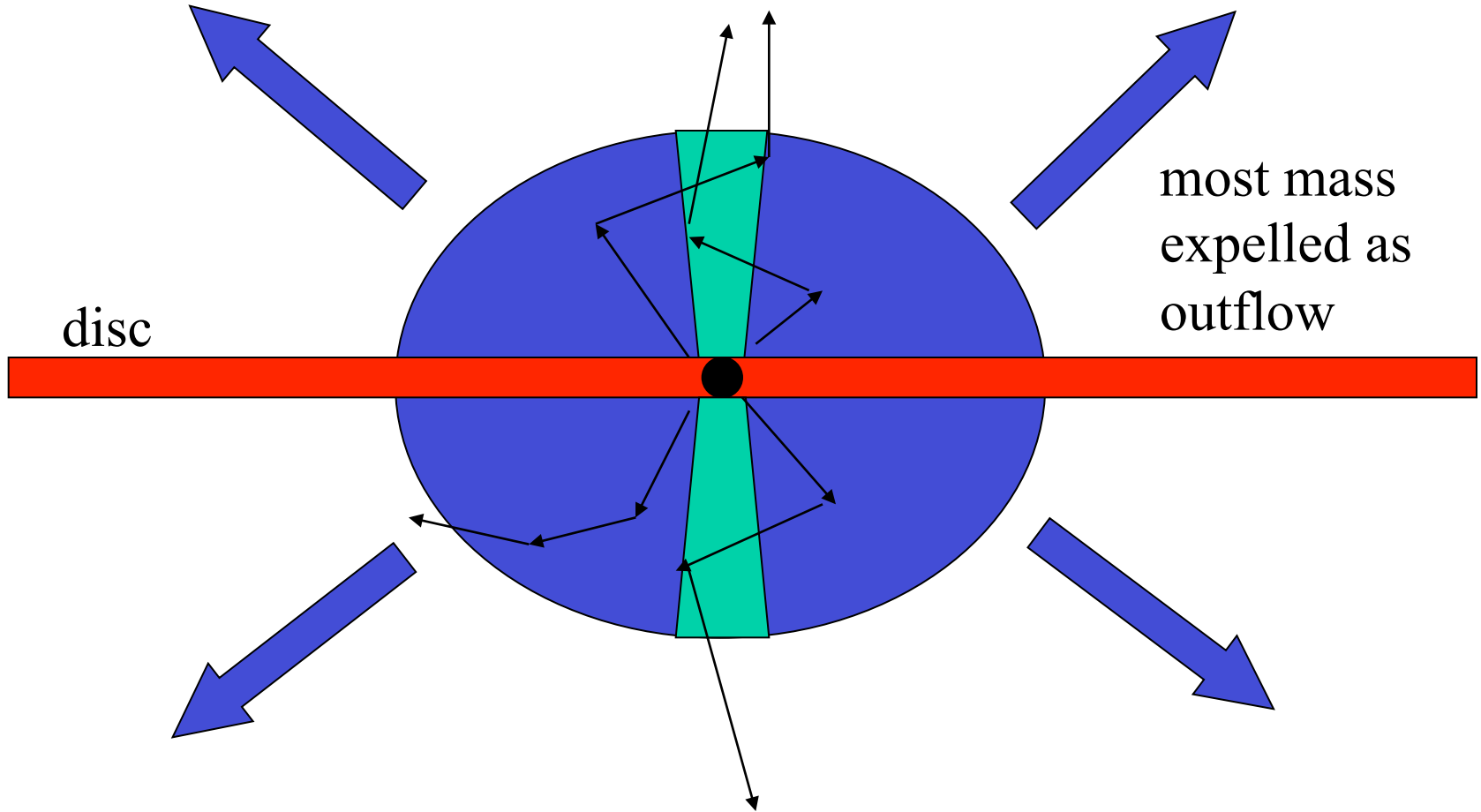


# Super-Eddington Accretion

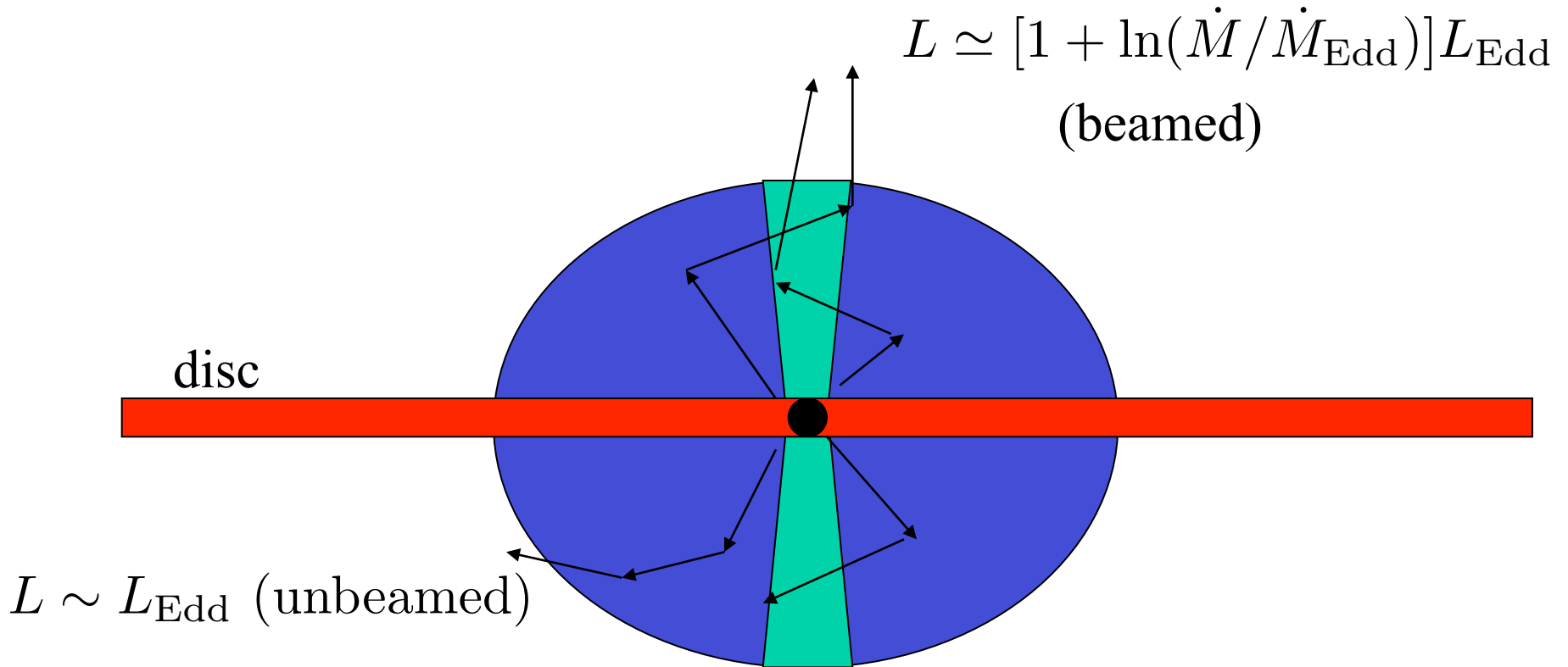


# Super-Eddington Accretion

most photons eventually escape along cones near axis: **jets**

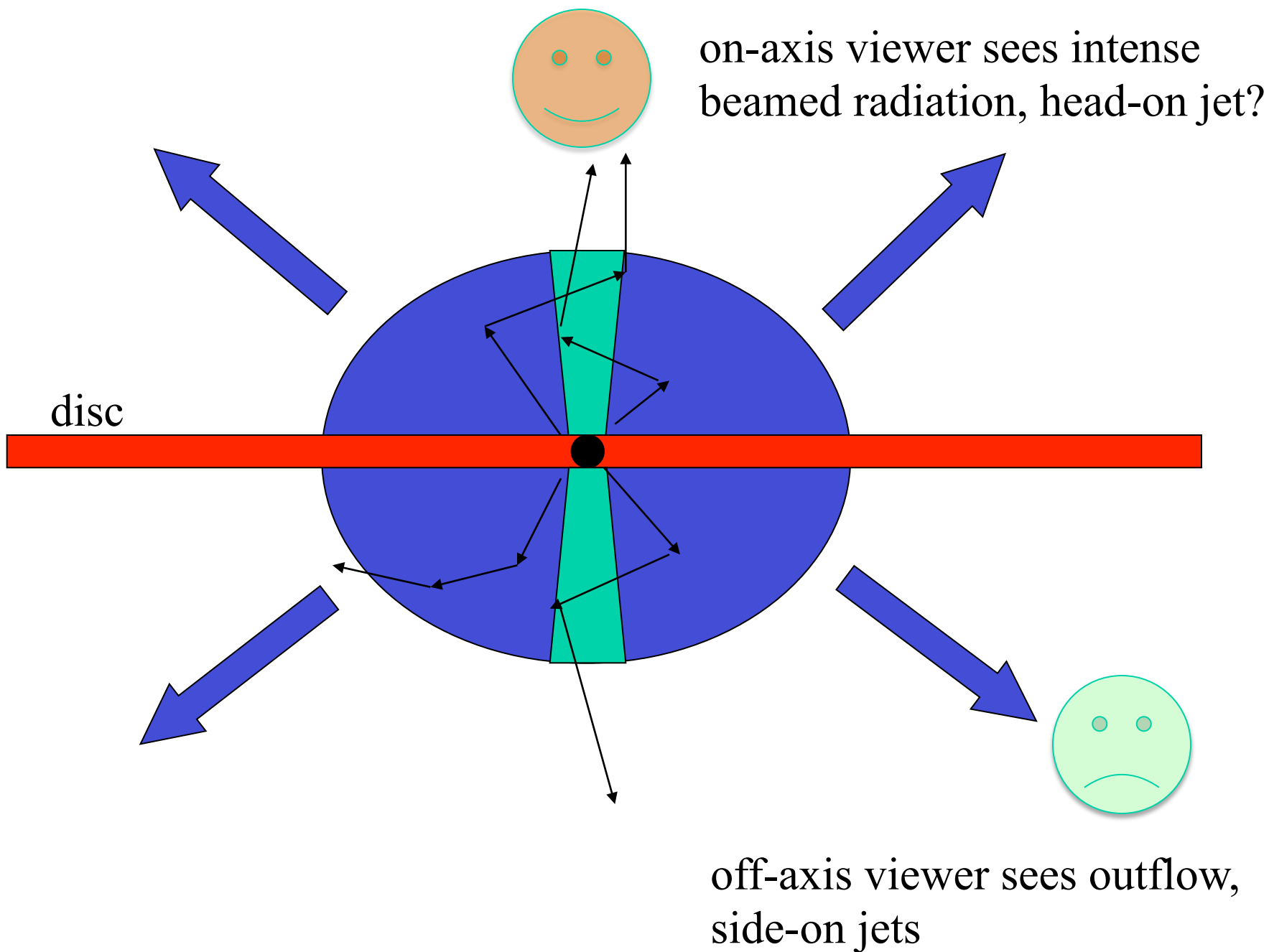


# Super-Eddington Accretion



local Eddington limit requires  $\dot{M}(R) = \dot{M}_{\text{Edd}} \frac{R}{R_{\text{sph}}}$ , where

$R_{\text{sph}} \sim (\dot{M} / \dot{M}_{\text{Edd}}) R_s$ ,  $R_s =$  Schwarzschild radius – most matter expelled here





off-axis viewer sees outflow, side-on jets: SS433

(cf Begelman, King & Pringle, 2006)

on-axis viewer sees intense beamed radiation

ultraluminous X—ray source = ULX

don't need exotic objects (e.g. intermediate-mass black holes)  
to make *most* ULXs, but just  $\dot{M} \gg \dot{M}_{\text{Edd}}$

this happens naturally in various stages of binary evolution

e.g.  $\sim$  every high-mass XRB probably becomes a ULX (like SS433)  
similarly, most ultracompact binaries start as ULXs

ULXs don't have to be black holes, just super-Eddington!

correlation  $L_{\text{obs}} \propto T^{-4}$  is observed for blackbody component of many ULXs (Kajava & Poutanen, 2009)

suggests beaming goes as

$$b \propto r^{-2} \propto \dot{M}^{-2}$$

(recall that  $R_{\text{sph}} \propto \dot{M} R_s$ )

ULX luminosity is

$$L_{\text{obs}} = \frac{L_E}{b} [1 + \ln(\dot{M} / \dot{M}_E)]$$

where  $b$  is beaming factor, set by inflow geometry.

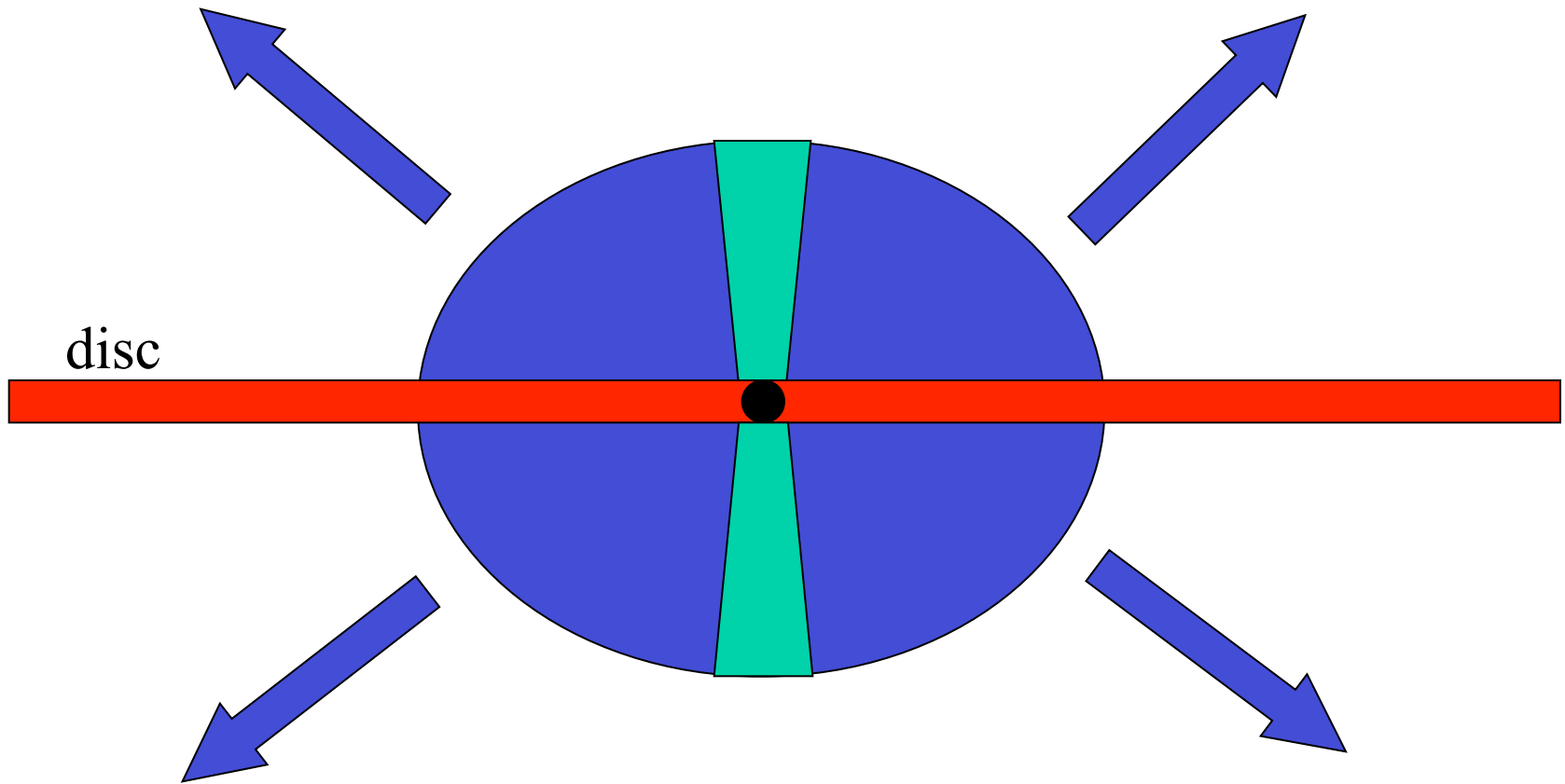
consider intrinsic blackbody emission from source near BH,

luminosity  $L_{bb} = lL_E$ , size  $R = rR_s \propto rM$

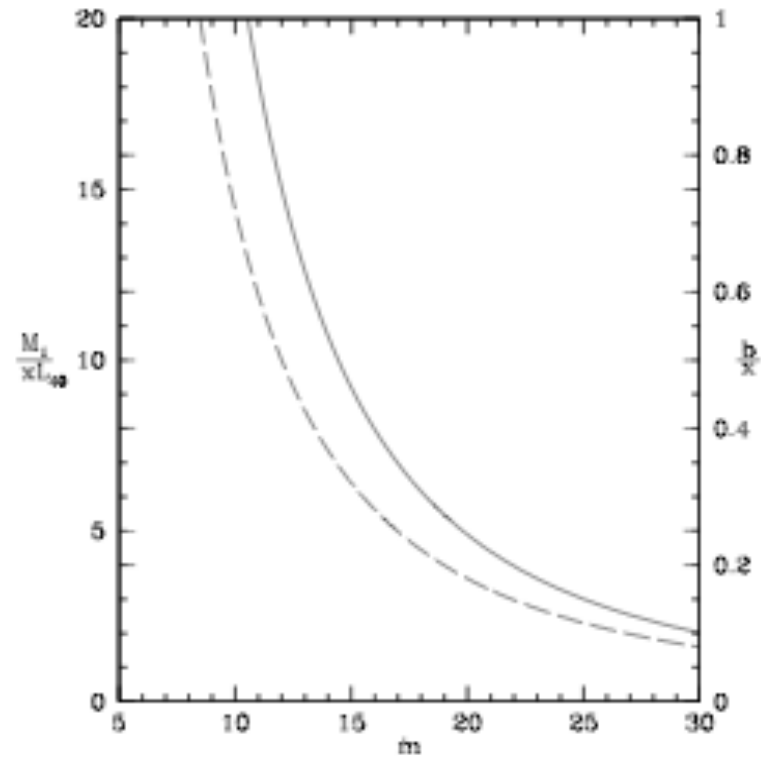
find  $L_{bb} \propto R^2 T^4 \propto r^2 M^2 T^4 \propto L_{bb}^2 T^4 \frac{r^2}{l^2}$

so

$$L_{\text{obs}} = \frac{1}{b} L_{bb} \propto T^{-4} \frac{l^2}{r^2 b}$$

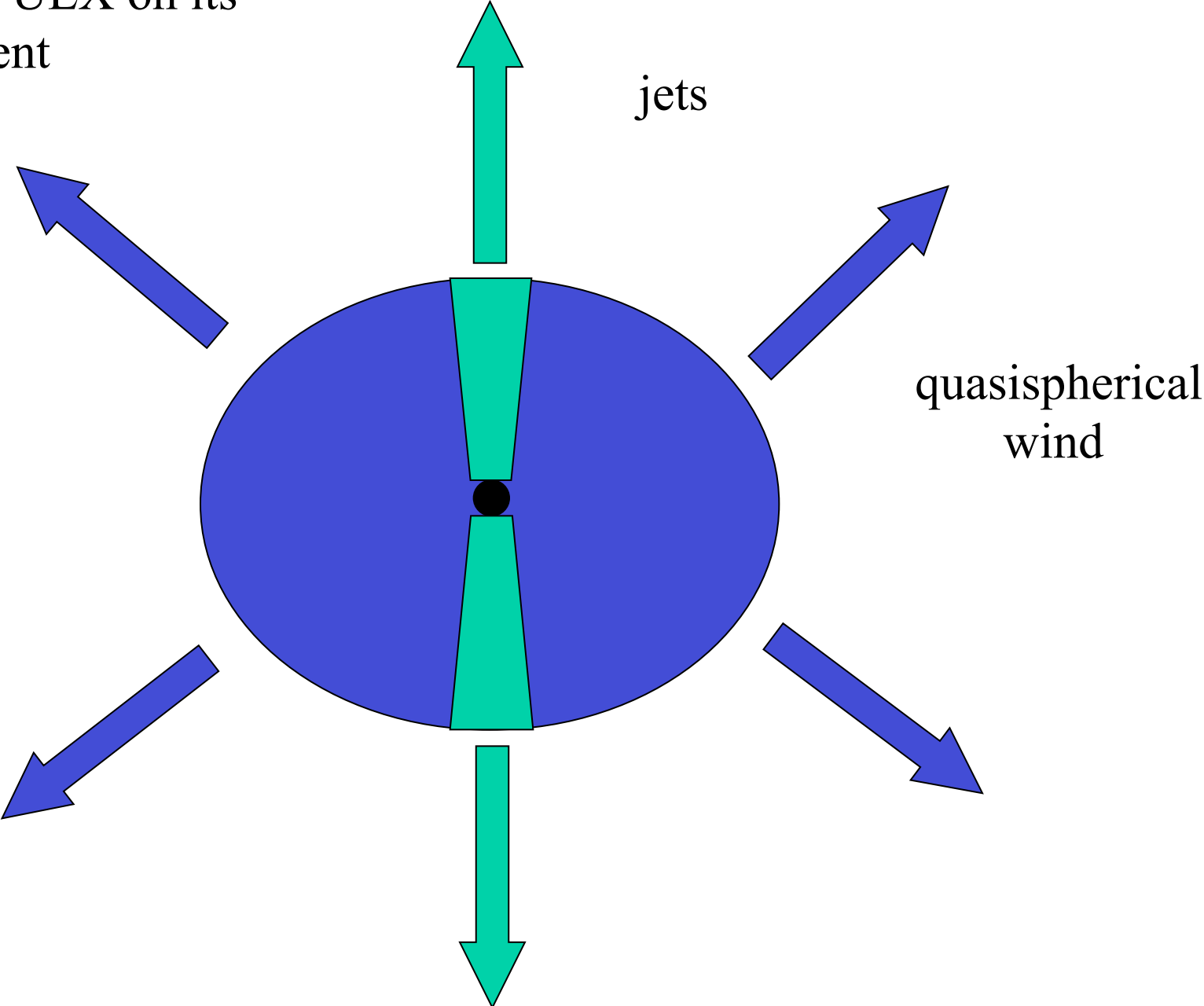


physically reasonable, as central structure is always Eddington  
but physical scale of funnel area goes as  $r^2 \propto \dot{M}^2$ , cf 'Polish  
doughnuts'



**Figure 1.** Beaming factor  $b$  (dashed curve) and accretor mass  $M_1$  (solid curve, in  $M_\odot$ ) as functions of the Eddington ratio  $m$  for ULXs. Here  $L_{40}$  is the inferred isotropic bolometric luminosity in units of  $10^{40}$  erg  $s^{-1}$  and  $x \sim 1$  a dimensionless quantity given by equation (7)

effect of a ULX on its environment



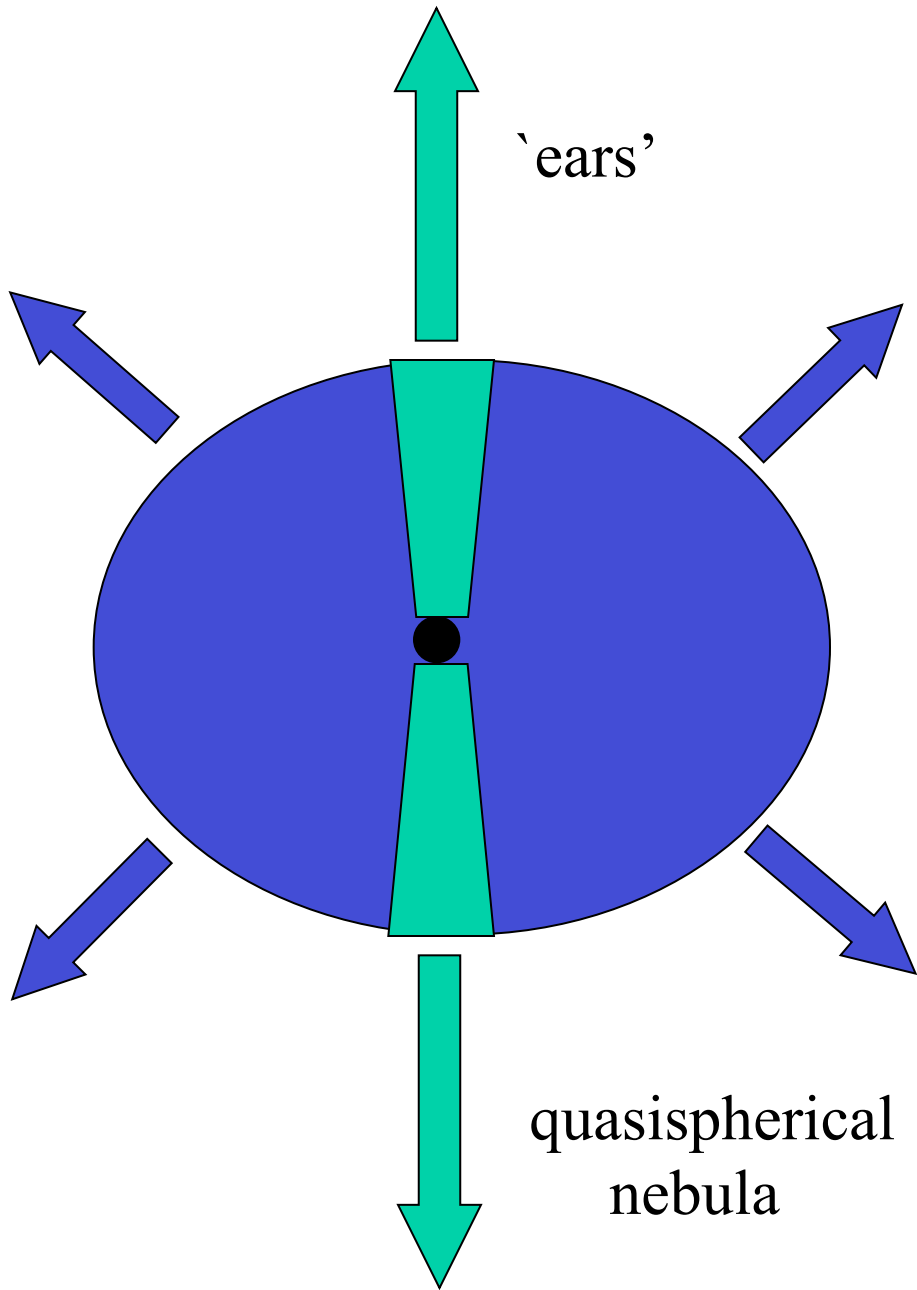
jets

quasispherical  
wind

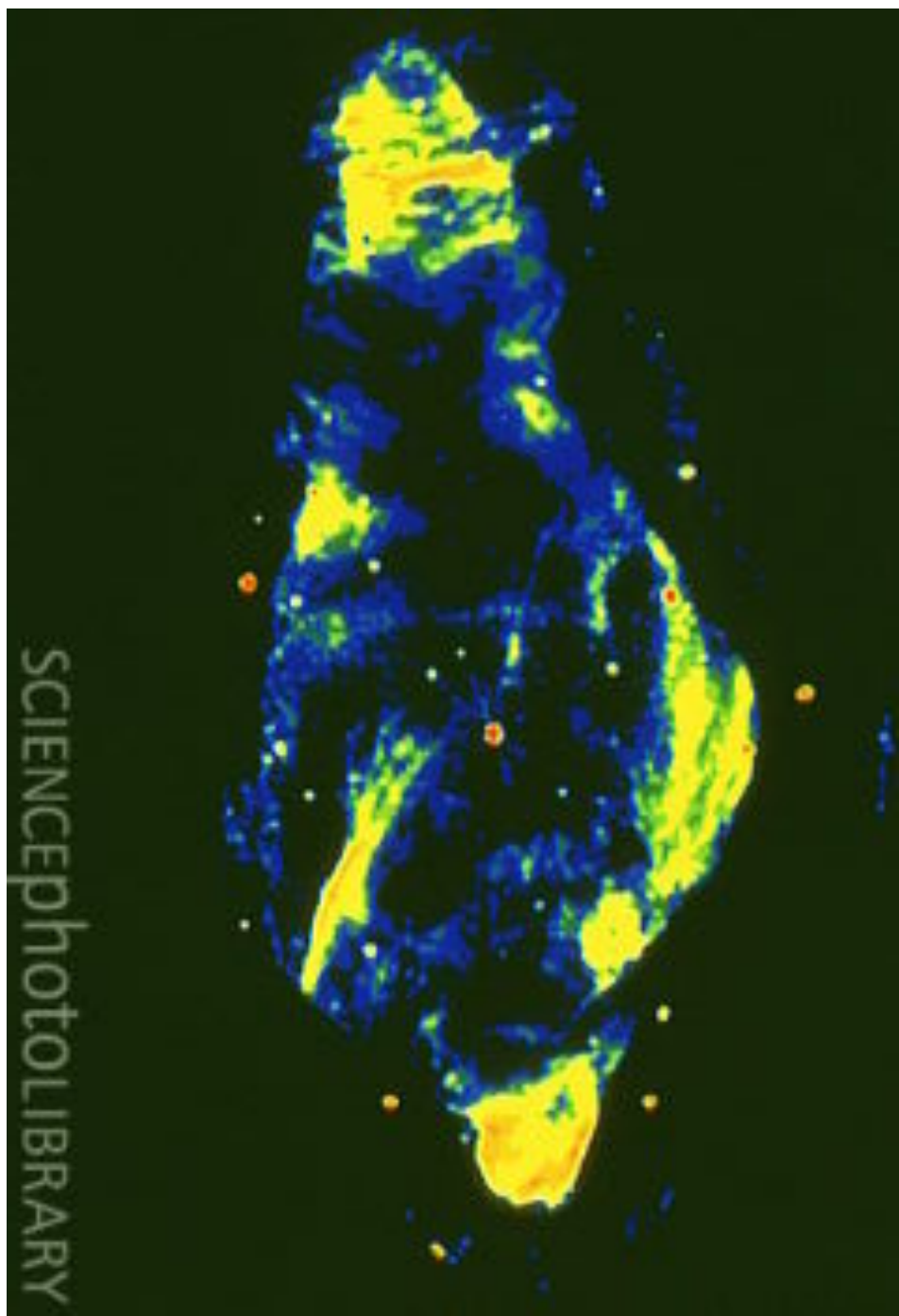
SS433 and W50

'ears'

quasispherical  
nebula



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*are there supermassive analogues of ULXs?*

how super—Eddington can an AGN BH be?

in virial equilibrium, mass inside radius  $R$  obeys  $GM/R \propto \sigma^2$

with  $\sigma =$  velocity dispersion of host galaxy

hence a gas mass  $M \sim f_g \sigma^2 R/G$  can fall in, on a timescale

$t \sim R/\sigma$ , so maximum accretion rate is

$$\dot{M}_{\text{dyn}} \sim \frac{f_g \sigma^3}{G}$$

compare with Eddington accretion rate  $\dot{M}_{\text{Edd}} \sim \frac{4\pi GM}{\kappa \eta c}$



→ Eddington ratio

$$r_{\text{Edd}} = \frac{\dot{M}_{\text{dyn}}}{\dot{M}_{\text{Edd}}} = \frac{f_g \sigma^3 \kappa \eta c}{4\pi G^2 M} = \frac{\eta c}{4\sigma} \simeq 50 \frac{\eta_{0.1}}{M_8^{1/4}},$$

using M—sigma relation  $M \simeq \frac{f_g \kappa}{\pi G^2} \sigma^4$

hence *AGN have only modest Eddington ratios:*

leads to M – sigma relation (King 2003, 2005)

as quasispherical outflow shuts off accretion on to SMBH

*can AGN ever be more super—Eddington than this?*

for a star, the  $\dot{M} \sim \frac{\sigma^3}{G}$  argument produces

$$\dot{M} \sim \frac{M_2}{P}$$

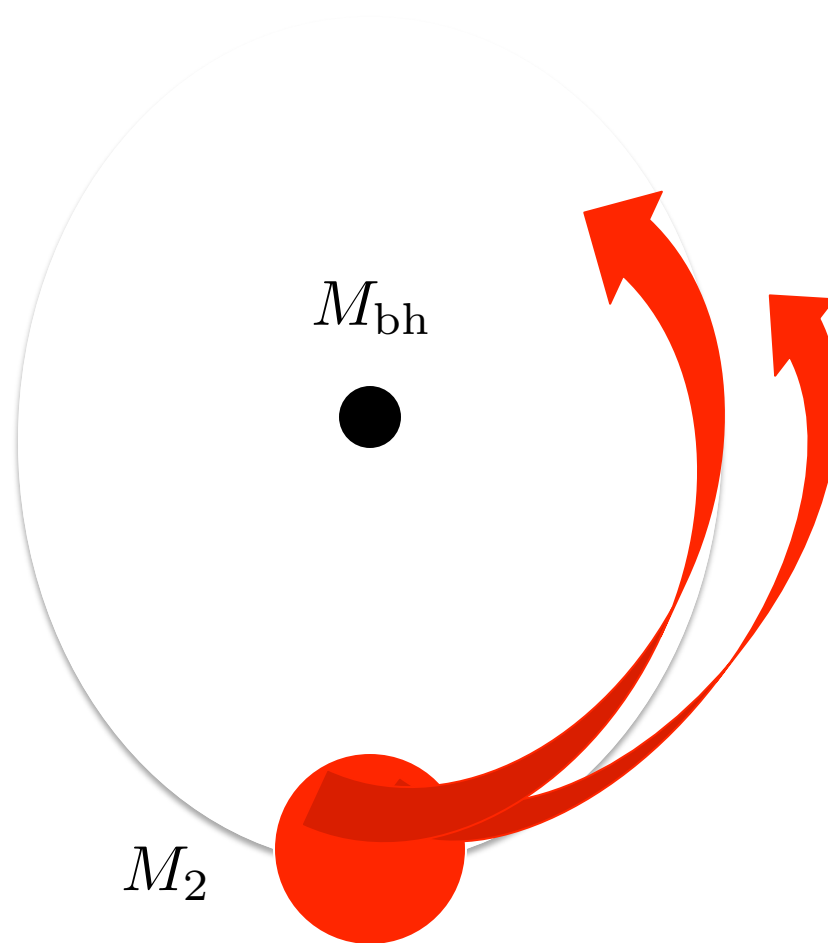
where P is the period of the circular orbit when star fills Roche lobe

this obeys  $M = 0.11 P_{\text{hr}} M_{\odot}$ , with  $P_{\text{hr}} =$  period in hours

this suggests  $\dot{M} \sim 10^4 M_{\odot} \text{ yr}^{-1}$

*but this is deceptive!*

in practice stars do not have circular orbits near a supermassive black hole, but are scattered in on near—parabolic orbits and disrupted at pericentre  $R = a$



half of star unbound from SMBH – bound half has a range of return times

$$T \sim \frac{2\pi GM_{\text{bh}}}{E^{3/2}}$$

where E is - orbital energy: this has a spread

$$E \sim \frac{GM_{\text{bh}}}{a^2} R_2$$

but tidal lobe filling at pericentre requires

$$\frac{R_2}{a} \sim \left( \frac{M_2}{M_{\text{bh}}} \right)^{1/3}$$

so spread in T is  $\sim P \left( \frac{M_{\text{bh}}}{M_2} \right)^{1/2} \sim 10^4 P$

hence in practice we get only  $\dot{M} \sim 1 M_{\odot} \text{ yr}^{-1}$

which is just Eddington for  $M_{\text{bh}} = 10^8 M_{\odot}$

tidal disruption requires  $M \lesssim \text{few} \times 10^6 M_{\odot}$  since otherwise star does not fill Roche lobe before accreting to SMBH

narrow parameter space for super—Eddington tidal disruption: is Sw 1644+57 (Bloom et al., 2011) this kind of event? distance  $\gg$  previous events: suggests *beaming* of HE emission – like ULX?

# Summary

- accretion is always via a disc – Bondi is never a good approximation
- thin  $\leftrightarrow$  Keplerian  $\leftrightarrow$  disc cools: theory incomplete (viscosity!)
- AGN disc:  $t_{\text{visc}} > t_{\text{H}}$  unless  $R < 1$  pc
- jets orthogonal to inner disc plane, not necessarily parallel to BH spin
- ULX beaming goes as  $b \propto r^{-2}$
- most ULXs are super-Eddington phase of close stellar—mass binaries
- ULX quasispherical winds  $\rightarrow$  nebulae
- AGN analogues of ULXs rare: tidal disruptions like Sw 1644+57



this leads to determinate equation for observed luminosity

$$L_{\text{obs}} = 2.2 \times 10^{36} m_1 \dot{m}^2 (1 + \ln \dot{m}) \text{ erg s}^{-1}$$

with  $m_1 = M_1/M_{\odot}, \dot{m} = \dot{M}/\dot{M}_E$

so accretor mass required to explain observed luminosity

$$L_{\text{obs}} = 10^{40} L_{40} \text{ erg s}^{-1}$$

is

$$\frac{m_1}{L_{40}} = \frac{4500}{\dot{m}^2 (1 + \ln \dot{m})}$$



so can explain most ULXs with stellar-mass binaries and modest Eddington factors (hence beaming)

not all ULXs must be black holes!

since  $\dot{M} = \dot{m}\dot{M}_E \propto L_E\dot{m} \propto (M_1/\eta c^2)\dot{m}$

where  $\eta$  is the efficiency (about 0.1 for both neutron stars and black holes, larger Eddington factor  $\dot{m}$  can compensate for smaller accretor mass, even with lower absolute accretion rate

thus a  $10M_\odot$  black hole with  $\dot{m} = 15$  produces same apparent luminosity as a  $1.4M_\odot$  neutron star with  $\dot{m} = 30$

neutron star has lower accretion rate (stronger beaming)  
white dwarf ULXs also possible (supersoft)

beaming – luminosity correlation now predicts **luminosity function**

nearest ULXs are at  $\sim 0.7$  Mpc, with luminosities  $\sim$  few times

$$10^{39} - 10^{40} \text{ erg s}^{-1}$$

agrees with observed LF (Mainieri et al., 2010)

NB ULXs in ellipticals *must be transient* (GRS 1915+105-like)  
since all HMXBs have disappeared since star formation

in spirals both types of ULXs can coexist

## pseudoblazars?

a ULX with the same Eddington factor as SS433 ( $\dot{m} \sim 3000 - 10^4$ )

would appear extremely bright — nearest would be at  $> 660$  Mpc,  
with apparent luminosity

$$L > 10^{45} \text{ erg s}^{-1}$$

-- right distance and luminosity for an AGN, but

*not centred on host galaxy* – e.g. PKS 1413 + 135?

## Summary

- stellar—mass binary can survive super—Eddington mass transfer by ejecting excess
- viewed off—axis these systems are like SS433, or X—ray transients
- viewed on—axis these are ULXs (‘SS433-like, GRS1915+105-like’)
- no need for exotic explanations (e.g. IMBH) – neutron star or even white—dwarf ULXs are possible
- beaming probably goes as  $b \propto \dot{m}^{-2}$  (Eddington factor) – LF agrees
- pseudoblazars possible
- no bright AGN analogues of ULXs